MENG366 System Dynamics and Control Laboratory Laboratory 10: Frequency response analysis using bode plot

1. OBJECTIVE

To analyze the stability of the given linear system using Bode plot .

2. COMPONENTS & EQUIPMENT

PC with MATLAB and Simulink toolbox installed.

3. BACKGROUND

The bode plot is a frequency response plot of the transfer function of a system. A bode plot consists of two graphs. One is plot of the magnitude of a sinusoidal transfer function versus $\log \omega$. The other is plot of the phase angle of a sinusoidal transfer function versus $\log \omega$. The main advantage of the bode plot is that multiplication of magnitude can be converted into addition. Also, a simple method for sketching an approximate log magnitude curve is available.

4. DESIGN PROCEDURE/ DESIGN CALCULATIONS:

The open loop transfer function of a unity feedback system:

$$G(s) = K/s(s^2 + 2s + 3)$$

- a) Draw the asymptotic Bode Plot to find:
 - (i) Gain Margin.
 - (ii) Phase Margin.
 - (iii) Gain cross over frequency.
 - (iv) Phase cross over frequency.
 - (v) Resonant Peak.
 - (vi) Resonant Frequency.
 - (vii) Bandwidth and check the same results using MATLAB Software. (Assume K=1)

- b) Use MATLAB and SIMULINK to find:
 - (viii) Gain Margin.
 - (ix) Phase Margin.
 - (x) Gain cross over frequency.
 - (xi) Phase cross over frequency.
 - (xii) Resonant Peak.
 - (xiii) Resonant Frequency.
 - (xiv) Bandwidth and check the same results using MATLAB Software. (Assume K=1)

MATLAB Program:

%Draw the Bode Plot for the given transfer functionG(S)=1/S(S2+2S+3) %Find (i)Gain Margin (ii) Phase Margin (iii) Gain Cross over Frequency %(iv) Phase Cross over Frequency (v)Resonant Peak (vi)Resonant %Frequency (vii)Bandwidth

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num=[1];
den=[1 2 3 0]; w=logspace(-1,3,100);
figure(1);
bode(num,den,w);
title('Bode Plot for the given transfer function G(s)=1/s(s^2+2s+3)) grid;
[Gm Pm Wcg Wcp] =margin(num,den);
Gain Margin dB=20*log10(Gm)
Phase Margin=Pm
Gaincrossover Frequency=Wcp
Phasecrossover Frequency=Wcg
[M P w]=bode(num,den);
[Mp i]=max(M);
Resonant PeakdB=20*log10(Mp)
Wp=w(i);
Resonant Frequency=Wp for
i=1:1:length(M);
if M(i) \le \frac{1}{(sqrt(2))};
Bandwidth=w(i)
break; end;
end;
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Prelab questions:

- Define frequency response analysis.
- What is the Gain margin and phase margin?

Postlab questions:

- What are the advantages and disadvantages of Bode plot?
- How can you analyze the stability of the system with Bode plot?